

27th International Conference on Flexible Automation and Intelligent Manufacturing,
FAIM2017, 27-30 June 2017, Modena, Italy

Using simulation to analyze picker blocking in manual order picking systems

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Abstract

The rise of the e-commerce practice makes the warehouses be confronted with ever smaller orders that must be met ever faster, often within a 24-h period. This pressures the order picking process as the orders pickers' workload becomes higher and higher, leading subsequently to congestion in the warehouse and impacting its productivity. It is therefore crucial to determine which order batching and picking policies enhance the performance of order picking activities. This paper carries out an intensive simulation study to examine the performance of different order picking policies with batching in a wide-aisle warehouse with a low-level picker-to-parts system. The performance of the system is measured in terms of total travelled distance, number of collisions between operators (congestion) and order lead times. A full factorial design is set up and the simulation output is statistically analyzed. The results are reported and thoroughly discussed.

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Peer-review under responsibility of the scientific committee of the 27th International Conference on Flexible Automation and Intelligent Manufacturing

Keywords: Order picking; Batching; Congestion; Simulation

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1. Introduction

Warehouses handle inbound functions such as receiving and preparing products for storage, transferring incoming products to storage locations, picking customer's orders from relevant locations, packing orders on the right unit load (e.g. a carton) and sending demands to destinations (De Koster et al. 2007). Across the various functions in a warehouse, order picking, referred to as the operation of retrieving the required stock keeping units (SKUs) from storage locations to fulfill customer orders, represents over 50% of the total operating cost in a common warehouse (Chiang et al. 2011; Frazelle 2001; Tompkins et al. 2010).

The nowadays fast growing e-commerce practice brings about new challenges for order picking activities. On the one hand, orders have to be met ever faster, often within a 24-h period. On the other hand, individual orders become smaller and smaller. An enormous number of low volume items have to be shipped more frequently and more quickly to clients (Gagliardi et al. 2008). Consequently, more pickers are involved in the picking process taking down order picking performance due to picker blockings (Hong 2015). De Koster and Yu (2006) state that congestion in distribution centers results in less worker productivity, more work stress and higher labor turnover. Moreover, the order fulfillment time can lengthen and operational costs increase.

The aim of this paper is to test and analyze the effect of different routing methods as well as order sequencing and storage strategies executed under different batching methods on low-level picker-to-parts picking performance. In particular, this paper adopts the order-batching methods developed by Ho and Tseng (2006) and carries out intensive simulations of these order-batching methods to evaluate the performance of warehouse picking operations, in terms of number of total distance travelled by operators, collisions between multiple pickers and order lead times (affected by congestion). The effects of different routing methods as well as order sequencing and storage strategies performing under these batching methods are also considered. Among different order picking systems, the most common is the low-level picker-to-parts system in which operators walk or drive (on a proper vehicle) along the aisle to pick items at multiple stops. De Koster et al. (2007) states that over 80% of all Western Europe warehouses implement low-level picker-to-parts picking systems. Therefore, this kind of system is the focus of this study.

The remainder of the paper is organized as follows. Section 2 provides a literature review on order picking operations and a motivation for carrying out these simulations. In Section 3, the problem environment and assumptions are described. Section 4 describes the experimental setup performed to evaluate different warehouse strategies taking picker congestion into account. It also summarizes the analyzed experimental results. Section 5 presents some conclusions and recommendations for further research.

2. Literature review and motivation

The existing research on order picking is quite extensive and various topics have been addressed by different authors. The published contributions in this area focus mainly on the following issues impacting the performance of the order picking system: layout of the warehouse, storage strategy, routing and sequencing policy and order batching. The layout of a warehouse is among the important factors influencing the performance of the order picking system. A study by Caron et al. (2000) has shown that the layout of a warehouse can have an impact of more than 60% on the total travelled distance. Moreover, determining the proper locations of items in the warehouse, i.e. storage assignment, is also a well-researched topic by, among others, (Ene and Öztürk 2012; Li et al. 2015; Manzini et al. 2015; Fontana and Nepomuceno 2016). The effect of order sequencing and routing on order picking performance is also widely studied in the literature (Chen et al. 2014; Kulak et al. 2012; Roodbergen and de Koster 2001). The simulations carried out in this paper provide some results on these effects.

Order batching, which has proven to have a significant impact on order picking (Ruben and Jacobs 1999), is the process of grouping customer orders together and picking them in the same tour. In such methods, orders are grouped into batches. Orders are assigned to a specific batch until the capacity of the batch is exhausted. A variety of approaches have been used to compose order batches. These approaches are based on (i) exact, (ii) heuristic, and (iii) metaheuristic methods (Henn et al. 2012).

This paper adopts the second method of order batching based on heuristic seed algorithms. Seed algorithms were introduced by Elsayed (1981) and generate batches sequentially. These algorithms consist of two distinct steps: seed order selection and order addition. In a first phase, one customer order is selected as an initial order (seed) for a batch which has just been opened. Afterwards, in the order addition phase, customer orders which are "similar" to

the seed, are added to the batch while taking the capacity of the picking device into account. One of the most comprehensive seed algorithm was proposed by Ho and Tseng, (Ho and Tseng 2006) where the authors consider 9 rules to determine the seed order and 10 criteria to allocate orders to batches. Section 3.1 provides a brief review of this approach.

Until recently, most of the previous studies in picker-to-parts warehousing systems considered only single-picker operations. However, it is a very common situation that multiple order pickers work concurrently within the same picking area. Worker interaction in the same space may sometimes lead to congestion, which reduces worker's productivity, and in turn increases labor costs (Gue et al. 2006). There are several contributions in literature related to picker blocking and congestion occurring in a warehouse (Gue et al. 2006; Pan et al. 2012; Hong et al. 2012a; Hong et al. 2012b). However, those researchers who have considered congestion in their work, mostly have presented mathematical models. The difficulty of using mathematical models in this field, however, stems from the nature of congestion which is a dynamic feature and hard to capture.

In this paper, we analyze congestion using simulation to get better insight. With simulation many alternative solutions can be tested quickly and easily, with little risk and no disruption to existing processes (Banks et al. 2010). Thus, simulation provides a tool to quantify the impact of congestion, while the various congestion factors and operating conditions change over time. This paper carries out intensive simulations of several heuristic batching methods described in Ho and Tseng (2006). It combines various storing, sorting and routing policies to compare and analyze the performance of a low-level picker-to-part order picking system. It focuses in particular on the congestion resulting from multiple pickers in a warehouse. The measures of performance that considered in this investigation are total distance travelled by order pickers, number of collisions between pickers and order lead times. The latter being influenced by congestion.

3. Problem environment and description

The warehouse investigated in this paper is a low-level picker-to-parts manual order picking system, as presented in Fig. 1. The layout structure is composed of 10 parallel wide aisles which are indexed from 1 to 10, and each aisle has 30 picking locations. Operators are able to move within an aisle in both directions and are allowed to change their direction within an aisle. The aisles are wide enough such that operators can cross each other. At the front and back of the aisles there are cross aisles to switch from one pick aisle to another pick aisle. The start station is located at the bottom left corner of the first aisle. Order pickers begin at the start station where they collect pick lists as well as carts. Then, they walk through the picking area and retrieve items from different slots. After finishing all picks, they go to the sorting platform where the items are left for shipping (sort-after-pick). The warehouse uses a wave picking policy, i.e. when a large set of customer orders is assigned to a pre-defined shipping schedule (called wave), all requested items must be picked and shipped within the corresponding wave. Each wave typically is a combination of a number of batches which are picked simultaneously by a group of order pickers (Gademann et al. 2001). Every order picker picks one batch and all order pickers start at the same time. In this paper, it is assumed that at the beginning of a wave, the set of orders that needs to be picked in the wave (order pool) is already known, and the orders are randomly generated. The distribution of the set of orders in the wave is done according to the type of storage policy, which will be explained later in more details. Before a wave begins, the set of orders in the order pool are grouped in batches, based on one of the batching methods proposed by (Ho and Tseng 2006) briefly reviewed in section 3.1. Then, each batch is assigned to one order picker who is ready to start his trip at the start station. It is assumed here that the size of each batch, defined as the number of items, is not greater than the picking cart's capacity, which is 100 items. Another assumption is that one order is not split into different batches to avoid additional sorting efforts and the time needed to wait until an order is completed by a number of operators. The wave is started when all batches are assigned to order pickers. At this point, pickers receive their pick lists (a pick list is a batch) which describe the storage locations that are to be visited and the corresponding number of items requested for each sku. The picking routes are determined by one of the routing methods considered, as explained in the next subsection. As mentioned, this paper addresses a warehouse with multiple pickers working concurrently in the same area, generating inevitably congestion. In the studied warehouse, congestion can occur in three ways: (i) when two or more pickers reach to the same picking face and attempt to occupy the same space simultaneously ; (ii) when a picker enters an aisle to retrieve items while the aisle is occupied by other pickers in a way that they cannot pass each other (iii) when blocking occurs in cross aisles.

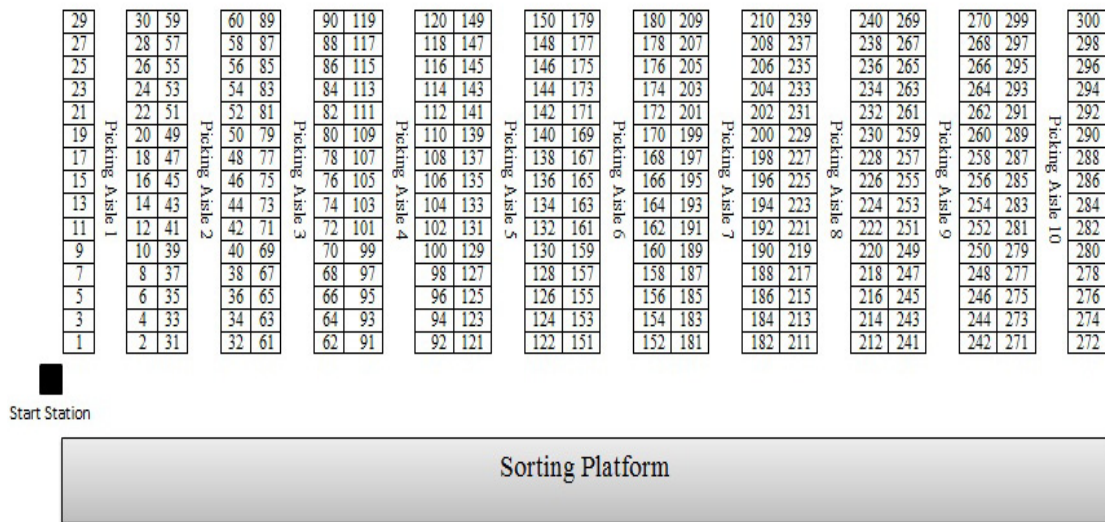


Figure 1. Warehouse layout

3.1 Batching Methods

For this study we adopt the order batching methods described in Ho and Tseng (2006). The authors implemented a seed algorithm to generate batches. They introduced 9 seed-order (SO) selection rules and 10 accompanying-order (AO) selection rules, summarized in following tables, to make a batch and assign it to a picker. The order-batching process to form an order batch works as follows: a seed order S is selected first from the order pool P using one of seed-order selection rules. The selected seed order is the first order added to the order batch B . Then the remaining capacity of the batch, RC , is updated by subtracting the capacity demand of the seed from the picking cart's capacity. After that, among all remaining orders with a capacity demand smaller than or equal to RC (set QS), an order is chosen based on an accompanying-order selection rule and is added to the order batch. Next, the remaining capacity of the picking cart is updated again, and the accompanying-order selection process is repeated until the picking cart is full and cannot accept any more orders. At this point, the first batch has been prepared and is assigned to the first picker. The same procedure is repeated for the next batch and next picker until all orders are batched.

Table 1. Summary of seed order (SO) selection rules. (see Ho and Tseng, 2006, for more details)

Seed-order selection rules	Definition
Random(RD)	The SO is randomly selected from the order pool.
Smallest N° of Picking Locations (SNPL)	The order which has the smallest number of picking locations to visit is selected as the SO.
Greatest N° of Picking Locations (GNPL)	The order which has the greatest number of picking locations to visit is selected as the SO.
Smallest N° of Picking Aisles (SNPA)	The order that has the smallest number of picking aisles to visit is selected as the SO.
Greatest N° of Picking Aisles (GNPA)	The order that has the greatest number of picking aisles to visit is selected as the SO.
Smallest Location-Aisle Ratio (SLAR)	For every order in the order pool, LAR (Location-Aisle Ratio) is: $LAR(R) = \frac{Nof PL(R)}{Nof PA(R)}$ where $Nof PL(R)$ = the number of picking locations of order R ; $Nof PA(R)$ = the number of picking aisles of order R . The order with the smallest LAR is selected as the SO.
Greatest Location-Aisle Ratio (GLAR)	Opposite to the SLAR rule, one selects the order with the greatest LAR as the SO.
Smallest Aisle-Weight Sum (SAWS)	For every order in the order pool, AWS (Aisle-Weight Sum) is: $AWS(R) = \sum_{i \in AS(R)} AW_i$ where i = aisle index; $AS(R)$ = the set of aisles that contain the items of order R ; $AW_i = 2^i$ (the farther away from the I/O, the greater an aisle's weight AW_i) The order with the smallest AWS is selected as the SO.
Greatest Aisle-Weight Sum (GAWS)	Opposite to the SAWS rule, one selects the order with the greatest AWS as the SO.

Table2. Summary of accompanying rules(AO). (see Ho and Tseng, 2006, for more details)

Accompanying-order selection rules	Definition
Random(RD)	The AO is randomly selected from the order pool.
Smallest N° of Additional Picking Locations (SNAPL)	The order with smallest number of additional picking locations, if order R is added to batch B, is selected as the AO.
Smallest N° of Additional Picking Aisles (SNAPA)	The order with the smallest number of additional picking aisles, if order R is added to batch B, is selected as the AO.
Greatest N° of Identical Picking Locations (GNIPL)	The order with the highest similarity to the batch, in terms of picking locations, is selected as the AO.
Greatest N° of Identical Picking Aisles (GNIPA)	The order with the highest similarity to the batch, in terms of picking aisles, is selected as the AO.
Greatest Picking-Location Similarity Ratio (GPLSR)	The order with the greatest PLSR, is selected as the AO: $PLSR(R, B) = \frac{NIPL(R, B)}{TNoPL(R, B)}$ where $NIPL(R, B)$ = number of identical picking locations between order R and the orders in B; $TNoPL(R, B)$ = total number of picking locations that the picker needs to visit if R is added to B.
Greatest Picking-Aisle Similarity Ratio (GPASR)	The order with the greatest PASR, is selected as the AO: $PASR(R, B) = \frac{NIPA(R, B)}{TNoPA(R, B)}$ where $NIPA(R, B)$ = number of identical picking aisles between R and the orders in B; $TNoPA(R, B)$ = total number of picking aisles that the picker needs to visit if R is added to B.
Greatest Picking-Location Covering Ratio (GPLCR)	The order with the greatest PLCR, is selected as the AO: $PLCR(R, B) = \frac{NIPL(R, B)}{NoPL(R, B)}$ where $NIPL(R, B)$ = number of identical picking locations between R and the orders in B; $NoPL(R, B)$ = number of picking locations of order R.
Greatest Picking-Aisle Covering Ratio (GPACR)	The order with the greatest PACR, is selected as the AO: $PACR(R, B) = \frac{NIPA(R, B)}{NoPA(R, B)}$ where $NIPA(R, B)$ = number of identical picking aisles between R and the orders in B; $NoPA(R, B)$ = number of picking aisles of order R.
Greatest Identical-Location to Additional-Aisle Ratio (GILAAR)	The order with the greatest ILAAR, is selected as the AO: $ILAAR(R, B) = \frac{NIPL(R, B)}{NAPA(R, B)}$ where $NIPL(R, B)$ = number of identical picking locations between R and the orders in B; $NAPA(R, B)$ = number of additional picking aisles that the picker needs to visit if R is added to B.

3.2 Routing policy

The objective of routing policies is to sequence the items on the pick list to ensure a good route through the warehouse. Two order picking policies are considered in this study:

S-shape routing: This means that any aisle containing at least one pick is traversed entirely (except potentially the last visited aisle). Aisles without picks are not entered. From the last visited aisle, the order picker returns to the sorting platform.

Return method: With this method an order picker enters and leaves each aisle from the same end. Only aisles with picks are visited.

3.3 Sorting methods

Sorting methods describe how the items in an order are sorted and the sequence of locations visited by an order picker. The three considered methods in this study are:

No sorting: The items are not sorted. As a consequence, the order picker may visit the same aisle multiple times.

Random aisle: The list of items is only sorted based on aisle. Items within the same aisle are grouped together and sorted such that the item closest to the order picker is picked first. The order picker can visit each aisle at most once. However, the sequence in which the aisles are visited is not sorted.

Completely sorted: The items are sorted by aisle as described above, and, moreover, the sequence of the aisles visited is sorted from left to right. Aisles with no items to pick are skipped.

3.4 Storage assignments

To evaluate whether the assignment of storage space has any influence on the performance of the system, two sets of orders are generated according to two types of storage policies. In the first set, it is assumed that the locations of the items are random and orders are randomly distributed throughout the entire warehouse. This means that every aisle has the same chance to be visited. However, in the second set we assume that popular items are placed in the aisles closest to the start station. The top 50% of the most popular items are randomly distributed in aisles 1, 2 and 3; aisles 4, 5, 6 and 7 store the next 30 % of items; and the remaining items are randomly distributed in aisles 8, 9 and 10. This is called class-based storage.

4. Simulation and results analysis

4.1 The simulation model

All experiments are simulated with Flexsim 7.5 software. The objective of the simulation is to capture the effect of the different batching, routing, storage policies and sorting methods on congestion. Aside from the number of collisions, the total travelled distance and the order lead times are also studied. The layout of the warehouse considered in the simulation is shown in Fig. 1. The width of every aisle within the warehouse is 2 meters. The speed of the operators is assumed to be 1 m per second. Each operator can operate one cart which has a capacity of 100 units. To provide a better basis for analyzing the system, 10 Order pools have been generated randomly in this study. Each order pool contains 75 orders and the number of different items in an order is uniformly generated from 1 to 20. In addition the quantity of each requested item varies from 1 to 4. Finally, it is assumed that there are enough operators to pick all requested items. Table 3 summarizes the full factorial design of experiments.

Table 3. Factors considered in the experiment

Seed Order (SO)	Accompanying Order (AO)	Routing Policy	Sorting Method	Storage Assignment
RD	SNAPA	RETURN	NO SORTING	RANDOM
SNPL	SANAPL	S-SHAPE	RANDOM AISLE	CLASS- BASED
SNPA	GNIAPA		COMPLETELY SORTED	
GNPL	GNIPL			
GNPA	GPACR			
GAWS	GPLSR			
SAWS	GPASR			
SLAR	GPLCR			
GLAR	RD			
	GILAAR			

In total $(9 \times 10 \times 2 \times 3 \times 2) = 1080$ combinations of factors must be examined. Since each combination is replicated 10 times, a total of 10800 simulations were carried out.

4.2 Analysis of the results

The results are analyzed by ANOVA and presented in the following tables.

The results in table 4 indicate that, for the three performance measures, total travelled distance, number of collisions, and order lead time, all of the main factors are significant at an α of 0.05. In addition, for travel distance, three of the ten two-way interactions and one of the three-way interactions are significant at an α of 0.05. In terms of collisions, four two-way interactions and one of the three-way interactions are significant at an α of 0.05. For order lead time, three of two-way interactions and one of the three-way interactions are significant at level of 0.05. Tables 4 , 5 and 6 present the mean for all three measures of performance and the 95% confidence interval for order-picking routing,

storage assignment and sorting rules respectively.

Table 4. Full factorial ANOVA

	Total travelled distance			Number Of Collisions			Order Lead Times		
	Mean Square	F	Sig.	Mean Square	F	Sig.	Mean Square	F	Sig.
SO	1249046926	53.62	.000	11345332	132.54	.000	2233183604	61.57	0
AO	3.275E+10	1406	.000	8961665	104.69	.000	3.369E+10	104.6	0
Storage	157229384	6.750	.000	3761034	43.93	.000	494431165	13.63	0
Routing	1.143E+10	490.8	.000	657338071	7679.3	.000	494431165	43.93	0
Sorting	6.133E+11	26329	.000	6413378817	7492.8	.000	8.26E+10	22789	0
SO*AO	273736.9	.012	1.00	5512.36	.064	1.00	633837.334	.017	1
SO*Storage	954930.3	.041	1.00	19055.46	.223	.987	2631600.75	.73	1
SO*Routing	45021.312	.002	1.00	4510.188	.053	1.00	85377.572	.002	1
SO*Sorting	123171.2	.005	1.00	8728.733	.102	1.00	381378.88	.011	1
AO*Storage	1267770.5	.054	1.00	20512.29	.240	.989	3013586.9	.083	1
AO*Routing	53627.6	.002	1.00	85041.74	.993	.443	2271341.06	.063	1
AO*Sorting	7869479.93	.338	1.00	66972.15	.782	.724	6719237.55	.185	1
Storage*Routing	263220546.4	11.3	.001	2745569.55	32.075	.000	600688786.5	16.56	0
Storage*Sorting	912898626.3	39.19	.000	8590689.21	100.36	.000	1973881318	54.42	0
Routing*Sorting	1581508575	67.89	.000	160263102.2	1872.2	.000	963809637.1	26.57	0
SO*AO* Storage	153322.1	.007	1.00	5549.152	.065	1.00	420266.54	.012	1
SO*AO* Routing	12237.85	.001	1.00	2072.838	.024	1.00	67017.650	.002	1
SO*AO* Sorting	53519	.002	1.00	4136.021	.048	1.00	147608.55	.004	1
SO*Storage*Routing	15952.5	.001	1.00	2944.918	.034	1.00	57588.065	.002	1
SO*Storage*Sorting	135897.5	.006	1.00	8101.971	.095	1.00	310409.73	.009	1
SO*Routing*Sorting	14861.7	.001	1.00	3517.40	.041	1.00	114722.418	.003	1
AO*Storage*Routing	141994.2	.006	1.00	9805.393	.115	.999	609799.93	.017	1
AO* Storage*Sorting	494375.01	.021	1.00	12921.50	.151	1.00	1157275.25	.032	1
AO*Routing*Sorting	89517.5	.004	1.00	10557.18	.123	1.00	1157275.25	.032	1
Storage*Routing*Sorting	61684512.3	2.648	.071	3462511.86	40.45	.000	273070818	7.52	1
SO*AO* Storage*Routing	10135.14	.000	1.00	2894.58	.034	1.00	93549.84	.003	1
SO*Accompanying Order* Storage*Sorting	52852.5	.002	1.00	4004.866	.047	1.00	184399.9	.005	1
SO*AO* Routing*Sorting	7860.34	.000	1.00	1737.334	.020	1.00	56443.889	.002	1
SO*Storage*Routing*Sorting	24580.14	.001	1.00	3889.746	.045	1.00	153385.213	.004	1
AO*Storage*Routing*Sorting	22383.64	.001	1.00	5816.973	.068	1.00	123253.449	.003	1
SO*AO* Storage* Routing* Sorting	6952.616	.000	1.00	1798.779	.021	1.00	50741.086	.001	1

Table 5. Performance factor means and 95% confidence intervals of Return and S-shape.

Dependent Variable	Routing	Mean	Std. Error	Upper Bound	Lower Bound
Total travelled distance	RETURN	25348.874	65.676	24786.541	26908.613
	S-SHAPE	26256.368	65.676	26102.005	26966.449
Number Of Collisions	RETURN	1294.397	3.981	1286.593	1302.201
	S-SHAPE	800.982	3.981	793.177	808.786
Order Lead Time	RETURN	32896.859	81.956	32736.209	33057.509
	S-SHAPE	30487.619	81.956	30326.969	30648.269

Table 6. Performance factor means and 95% confidence intervals of CLASS-BASED and RANDOM.

Dependent Variable	Distribution	Mean	Std. Error	Lower Bound	Upper Bound
Total travelled distance	CLASS-BASED	26358.711	65.676	26185.500	27058.189
	RANDOM	26716.520	65.676	26559.395	26816.873
Number Of Collisions	CLASS-BASED	1066.351	3.981	1058.546	1074.155
	RANDOM	1029.028	3.981	1021.224	1036.833
Order Lead Time	CLASS-BASED	31906.203	81.956	31745.553	32066.853
	RANDOM	31478.275	81.956	31317.625	31638.925

Table 7. Performance factor means and 95% confidence intervals of Sorting methods.

Dependent Variable	Sorting	Mean	Std. Error	Lower Bound	Upper Bound
Total travelled distance	NO SORTING	42056.621	80.437	41671.913	42369.784
	COMPLETE SORTING	18197.548	80.437	18073.723	18389.069
	RANDOMLY SORTED	20450.698	80.437	20207.720	20598.145
Number Of Collisions	NO SORTING	1534.957	4.876	1525.399	1544.516
	COMPLETE SORTING	813.445	4.876	803.887	823.003
	RANDOMLY SORTED	794.666	4.876	785.107	804.224
Order Lead Time	NO SORTING	49149.373	100.375	48952.618	49346.128
	COMPLETE SORTING	21943.621	100.375	21746.866	22140.376
	RANDOMLY SORTED	23983.722	100.375	23786.967	24180.478

Table 8. Performance factor means and 95% confidence intervals of Seed order selection rules.

Dependent Variable	Seed Order	Mean	Std. Error	Lower Bound	Upper Bound
Total travelled distance	GAWS	28865.23	139.321	28317.853	28970.577
	GLAR	26765.25	139.321	26460.299	27006.493
	GNPA	27931.66	139.321	27409.379	27955.574
	GNPL	28118.33	139.321	27435.426	28467.714
	RD	26655.10	139.321	26271.063	26817.257
	SAWS	26384.92	139.321	25805.340	26445.017
	SLAR	26802.54	139.321	26486.253	27032.448
	SNPA	25844.56	139.321	25314.314	25860.509
	SNPL	25911.72	139.321	25321.321	25945.100
Number Of Collisions	GAWS	1104.036	8.446	1087.480	1120.591
	GLAR	1101.700	8.446	1085.144	1118.256
	GNPA	1099.092	8.446	1082.537	1115.648
	GNPL	1107.758	8.446	1091.202	1124.313
	RD	1210.036	8.446	1193.480	1226.591
	SAWS	950.909	8.446	934.354	967.465
	SLAR	956.941	8.446	940.385	973.496
	SNPA	949.028	8.446	932.473	965.584
	SNPL	949.705	8.446	933.149	966.261
Order Lead Time	GAWS	33756.12	173.854	33415.339	34096.920
	GLAR	31886.89	173.854	31546.106	32227.686
	GNPA	32822.93	173.854	32482.149	33163.729
	GNPL	32892.31	173.854	32551.521	33233.101
	RD	32239.33	173.854	31898.549	32580.129
	SAWS	30477.98	173.854	30137.193	30818.774
	SLAR	31189.05	173.854	30848.265	31529.845
	SNPA	29977.55	173.854	29636.763	30318.343
	SNPL	29987.94	173.854	29647.153	30328.734

From obtained results, it can be concluded that the RETURN method is considerably better than the S-SHAPE method in terms of travelled distance. However, for collisions and lead time, S-SHAPE routing outperforms the RETURN method. The reason is that in RETURN routing, order pickers collide when they return through the same

aisle, which results in delays, increasing the order lead times. From the table 6, one can conclude that the class based policy outperforms the random policy in total travelled distance. This was expected since top ranked items are placed in aisles close to the start station. On the other hand, implementing a class-based policy when more operators work in the same area, will increase the number of collisions within the warehouse as well as the order lead times.

Regarding the different sorting rules, of which factors' performance means and confidence intervals are indicated in table 7, it can be concluded that COMPLETE SORTING has the best performance in terms of travelled distance, followed by RANDOM and NO SORTING rule. Table 7 also reveals that if the NO SORTING rule is selected as sorting method, there will be a considerable rise in order lead times and collisions.

Based on the results of table 8, SNPA is the best method while GAWS is the worst one. It also can be seen that, among all nine seed rules, SNPA, SNPL, and SAWS have a better performance in total travelled distance. This means they are not significantly different (at an α of 0.05) in their performance, but they are all significantly better than the other seed-order selection rules at an α of 0.05. On the other hand, GNPA, GNPL and GAWS are the three worst rules. According to the analyzed results from tables 8, it can be noticed that SNPA, SNPL, SAWS and SLAR perform well in terms of both number of collisions and orders lead time, while GNPL, GAWS AND RANDOM perform poorly. Additionally, it can be concluded that the smallest value-based rules (i.e. SNPL, SNPA, SAWS, and SLAR) are all better than greatest value-based rules (i.e. GLAR, GNPL, GNPA, and GAWS). In addition, the RD rule is worse than the all greatest-value-based rules in collisions and order lead time. Table 9 presents the factors performance means of each accompanying order selection for total travelled distance, number of collisions and orders lead time respectively. From this table, one can notice that SNAPA has the best performance on total travelled distance and the RANDOM rule has the worse results. Table 9 also shows that all accompanying order rules are better than RANDOM rules in distance based performance. In addition, the top four rules (i.e. SNAPA, GNIPA, GPACR, and GILAAAR) are all related to aisle-based values.

5. Conclusion

The aim of this investigation is to study and analyze the performance of a low-level order picking warehouse when multiple operators work simultaneously. In our analysis, a wide range of designs were explored. The designs that we considered include the seed order batching method outlined in (Ho and Tseng 2006), three types of sorting methods, storage assignment rules and two routing policies. The experiments were carried out to measure warehouse performance in terms of total distance travelled by pickers, number of collisions among pickers and resulting order lead time including congestion effects. Simulation models were hired to determine the impact that various operating strategies may have on the warehouse and determine which ones are the best to pursue. In total 10800 simulation models were implemented and the results were analyzed via full factorial ANOVA. The results show that congestion has a direct impact on order lead time. Additionally, the experimental analyses discussed in this paper also provided the following conclusions.

The results also indicate that the best configuration for the total travelled distance is obtained using a return routing policy and class-based storage strategy while orders in picking lists are sorted in a way that all aisles and location within aisles are sequenced (in the studied case from left to right). Regarding the seed selection rules, the smallest value-based rules (i.e. SNPL, SNPA, SAWS, and SLAR) perform better than greatest value-based rules (i.e. GLAR, GNPL, GNPA, and GAWS) while, the RD rule performs poorly than all other rules for collisions and order lead time and outperforms greatest value-based rules in terms of total distance travelled. Concerning the accompanying rules, the best rule is Smallest Number of Additional Picking Aisles (SNAPA).

Table 9. Performance factors means and 95% confidence intervals of each accompanying-order selection rule.

Dependent Variable	AO	Mean	Std. Error	Lower Bound	Upper Bound
Total travelled distance	GILAAAR	23890.654	146.857	23453.129	24028.869
	GNIPA	19666.083	146.857	19509.139	20084.879
	GNIPL	26100.005	146.857	25531.613	26107.352
	GPACR	21726.396	146.857	21468.839	22044.579
	GPASR	32501.214	146.857	31711.681	32996.609
	GPLCR	32523.168	146.857	31723.881	32603.076
	GPLSR	30789.439	146.857	29671.370	31098.651
	RD	35790.380	146.857	34856.331	36905.466
	SNAPA	19465.654	146.857	19292.442	19868.182
	SNAPL	28411.932	146.857	27990.791	28709.543
Number Of Collisions	GILAAAR	1093.698	8.903	1076.247	1111.149
	GNIPA	1153.461	8.903	1136.010	1170.912
	GNIPL	1154.128	8.903	1136.677	1171.579
	GPACR	1054.614	8.903	1037.163	1072.065
	GPASR	1074.194	8.903	1056.743	1091.646
	GPLCR	1074.938	8.903	1057.487	1092.389
	GPLSR	1072.281	8.903	1054.829	1089.732
	RD	1001.337	8.903	983.886	1018.788
	SNAPA	870.346	8.903	852.895	887.797
	SNAPL	927.897	8.903	910.446	945.348
Order Lead Time	GILAAAR	28459.490	183.258	28100.265	28818.714
	GNIPA	24564.315	183.258	24205.090	24923.539
	GNIPL	30590.121	183.258	30230.897	30949.346
	GPACR	26579.779	183.258	26220.554	26939.003
	GPASR	36920.523	183.258	36561.299	37279.748
	GPLCR	36936.440	183.258	36577.216	37295.665
	GPLSR	34870.643	183.258	34511.418	35229.867
	RD	40150.886	183.258	39791.662	40510.111
	SNAPA	24432.044	183.258	24072.819	24791.268
	SNAPL	33418.147	183.258	33058.923	33777.372

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